

The DUNE PrismGrid Module

CHRISTOPH GERSBACHER

DUNE User Meeting
October 8, 2010 Stuttgart

Introduction

Design and Implementation of DUNE PrismGrid

Numerical Results and Applications

Conclusion

Introduction

Design and Implementation of DUNE PrismGrid

Numerical Results and Applications

Conclusion

Meta grids developed in Freiburg

- ▶ GeometryGrid (M. Nolte)
- ▶ IdGrid (M. Nolte)
- ▶ ParallelGrid (R. Klöfkorn)
- ▶ PrismGrid

Observations

- ▶ Easy to implement (?)
- ▶ Performance loss

Meta grids developed in Freiburg

- ▶ GeometryGrid (M. Nolte)
- ▶ IdGrid (M. Nolte)
- ▶ ParallelGrid (R. Klöfkorn)
- ▶ PrismGrid

Observations

- ▶ Easy to implement (?)
- ▶ Performance loss

Project History

- ▶ First version developed in 2008 (*2D unstructured simplex grids to 3D prismatic grid, suitable for parallel computations*)
- ▶ New generic version since 2009
- ▶ Project website launch in 2010
- ▶ For 2011: make module available

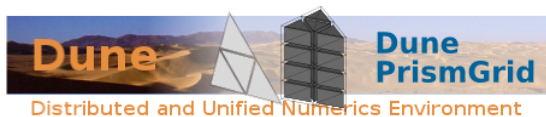


Figure: The DUNE PrismGrid logo

Features

- ▶ Generic prismatic elements over arbitrary d -dimensional DUNE grid (*the host grid*)
- ▶ Structured in vertical direction with flat upper and lower boundaries
- ▶ Periodic in vertical direction and horizontal directions (*if host grid is periodic*)
- ▶ Access to host grid

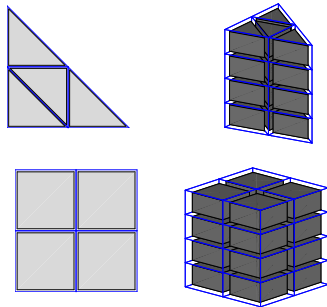


Figure: 2d host grids and resulting 3d prismatic grids

Features

- ▶ Access to several iterators for columns and layers
- ▶ Entities of all codimensions (*independent of the host grid implementation*)
- ▶ DGF support (*including IntervalBlock*)
- ▶ Two geometry implementations (*original implementation and generic geometries*)

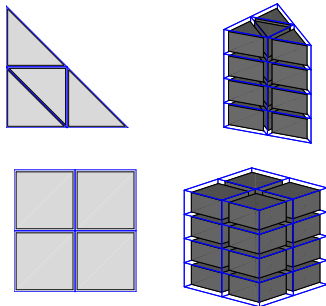


Figure: 2d host grids and resulting 3d prismatic grids

Open Issues

- ▶ Adaptivity
- ▶ Parallel support
- ▶ I/O
- ▶ Performance

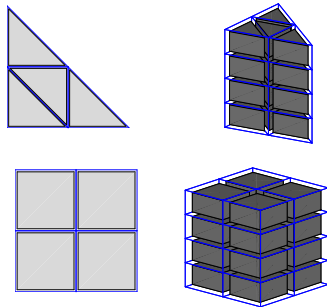


Figure: 2d host grids and resulting 3d prismatic grids

- ▶ New in DUNE 2.0: Generic reference elements
- ▶ Inductive construction rule (*pyramids and prisms*)
- ▶ In PrismGrid: Allows generic mapping from PrismGrid geometry types to host grid geometry types
- ▶ Generic Geometries

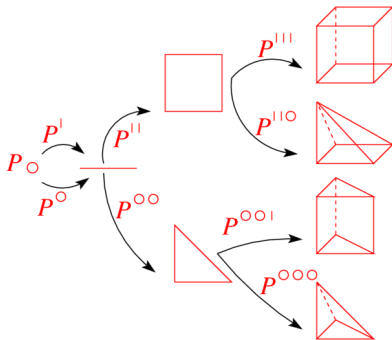


Figure: Construction of reference elements (A. Dedner)

Introduction

Design and Implementation of DUNE PrismGrid

Numerical Results and Applications

Conclusion

```

template< class HostGrid >
class PrismGrid
: GridDefaultImplementation < .. >
{
    ...

    // dimension of grid
    enum { dimension = HostGrid::dimension + 1 };

    // dimension of world
    enum { dimensionworld = HostGrid::dimensionworld + 1 };

    // constructor
    PrismGrid ( HostGrid * hostgrid, LineGrid * linegrid );

    // export type of underlying host grid
    typedef typename GridFamily::HostGrid HostGrid;
    HostGrid * hostGrid_;

    // type of line grid
    typedef typename GridFamily::LineGrid LineGrid;
    LineGrid * lineGrid_;

    ...
};

```

A LineGrid is a container of intervals with iterators and geometry:

```

template< class ctype >
class LineGrid
{
    // constructor
    LineGrid ( const int n, const ctype left, const ctype right,
              ...
              );

    // return iterator for given direction
    IteratorType iterator ( int direction ) const
    {
        if ( direction == 1 )
            return up_iterator();
        else
            return down_iterator();
    }

    // return end iterator for given direction
    IteratorType end_iterator ( int direction ) const;

    ...
}
    
```

A PrismGrid can be constructed from a DGF-file of the following form:

DGF

HOSTGRID

hostgrid.dgf % host grid dgf file

#

LINEGRID

0. 1. 2 % [0., 1.], 2 cells

55 66 % bottomId = 55, topId = 66

0 % no periodicity

#

The following GRIDTYPE typedefs are defined during `./configure`:

```
PRISMGRID_SGRID  
PRISMGRID_YASPGRID  
PRISMGRID_ONEDGRID  
PRISMGRID_ALBERTA  
PRISMGRID_ALUGRID_CONFORM  
PRISMGRID_ALUGRID_CUBE  
PRISMGRID_ALUGRID_SIMPLEX
```

Compile:

```
make GRIDTYPE=PRISMGRID_SGRID GRIDDIM=3 WORLDDIM=4 ...  
// host grid is SGRID< 3, 4 >
```

There are several possible iterators:

- ▶ Columnwise
- ▶ Layerwise
- ▶ From lower to upper
- ▶ From upper to lower

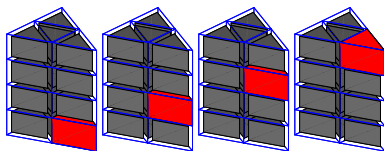


Figure: Iteration upwards a column

Which iterator shall be implemented / used / chosen?

There are several possible iterators:

- ▶ Columnwise
- ▶ Layerwise
 - ▶ From lower to upper
 - ▶ From upper to lower

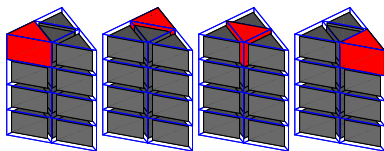


Figure: Iteration over top layer

Which iterator shall be implemented / used / chosen?

There are several possible iterators:

- ▶ Columnwise
- ▶ Layerwise
- ▶ From lower to upper
- ▶ From upper to lower

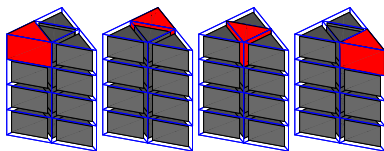


Figure: Iteration over top layer

Which iterator shall be implemented / used / chosen?

There are several possible iterators:

- ▶ Columnwise
- ▶ Layerwise
- ▶ From lower to upper
- ▶ From upper to lower

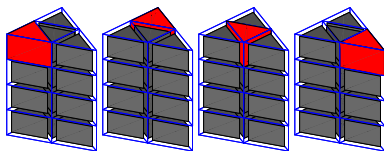


Figure: Iteration over top layer

Which iterator shall be implemented / used / chosen?

```

template< ... >
struct PrismGridSettings
{
    // define the iteration implementation to be used
    static const prismgrid::PrismGridIteratorImplementation
        IteratorImplementation = prismgrid::ColumnWise;
        // IteratorImplementation = prismgrid::LayerWise;

    // define the geometry implementation to be used
    static const prismgrid::PrismGridGeometryImplementation
        GeometryImplementation = prismgrid::OriginalGeometry;
        // GeometryImplementation = prismgrid::GenericGeometry;

    ...
};
  
```

- ▶ In many applications, the meta grid and the host grid are used simultaneously.
- ▶ The `HostGridAccess` structure makes the host grid available through the meta grid and gives access to host grid entities from meta grid entities.
- ▶ Meta grids implementing the host grid access: `GeometryGrid`, `IDGrid`, `PrismGrid`, ...

```

template< class HostGrid >
struct HostGridAccess< PrismGrid< HostGrid > >
{
    ...

    // return reference to host grid
    static const HostGrid & hostGrid ( const PrismGrid & grid )
    {
        return grid.hostGrid();
    }

    // get host grid entity
    template< class Entity >
    static const typename Codim< Entity::codimension >::HostEntity &
    hostEntity ( const Entity &entity );

    ...
};

```

Introduction

Design and Implementation of DUNE PrismGrid

Numerical Results and Applications

Conclusion

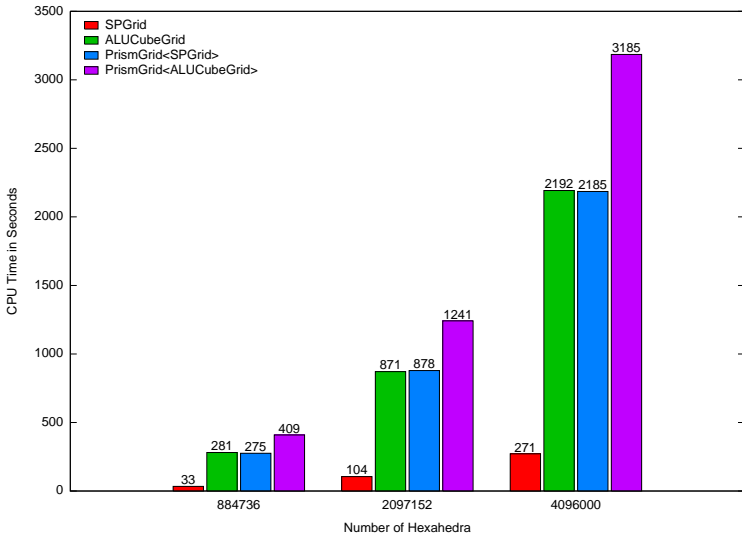
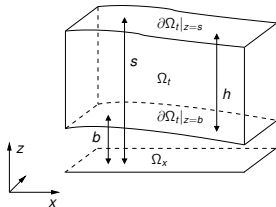


Chart provided by M. Nolte

- ▶ Geometry: Copy $d \times d$ -FieldMatrix into $(d + 1) \times (d + 1)$ -FieldMatrix for JacobianTransposed, JacobianInverseTransposed, ...
- ▶ Methods returning references
- ▶ Hold as few entity pointers as possible!

We consider the d -dimensional incompressible Navier-Stokes equations for shallow flows with a free surface ($d = 2, 3$):

$$\begin{aligned}
 \partial_t u_x + (u \cdot \nabla) u_x + \nabla_x p &= \mu \partial_z^2 u_x && \text{in } \Omega_t, \\
 \nabla \cdot u &= 0 && \text{in } \Omega_t, \\
 \partial_z p &= -g && \text{in } \Omega_t, \\
 \partial_t s + u_x \cdot \nabla_x s &= u_z && \text{on } \partial\Omega_t|_{z=s}, \\
 u_x \cdot \nabla_x b &= u_z && \text{on } \partial\Omega_t|_{z=b}, \\
 \mu \partial_z u_x &= 0 && \text{on } \partial\Omega_t|_{z=s}, \\
 \mu \partial_z u_x &= \kappa u_x && \text{on } \partial\Omega_t|_{z=b}.
 \end{aligned}$$



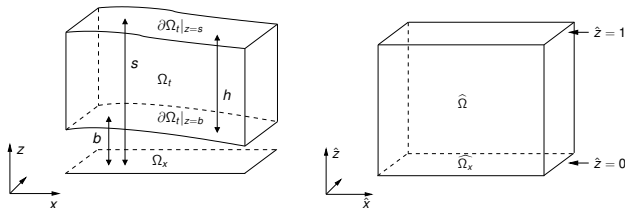
For the discretization, the so called σ -transformation is applied: Let

$$\hat{t} = t, \quad \hat{x} = x, \quad \text{and} \quad \hat{z} = \sigma(t, x, z) = \frac{z - b(x)}{h(t, x)}.$$

Then, for all times t it holds

$$\widehat{\Omega}_t = \{(\hat{x}, \hat{z}) \mid (x, z) \in \Omega_t\} = \widehat{\Omega}_x \times (0, 1),$$

i. e. the transformed domain is fixed in time.



- ▶ LDG solver in DUNE-FEM
- ▶ used an early version of PrismGrid
- ▶ combination of PrismGrid and GeometryGrid for visualization

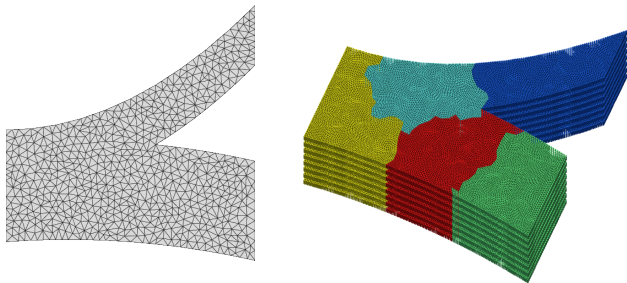


Figure: Two dimensional unstructured simplex grid (left) and resulting three dimensional prismatic grid with five partitions for parallel computations (right)

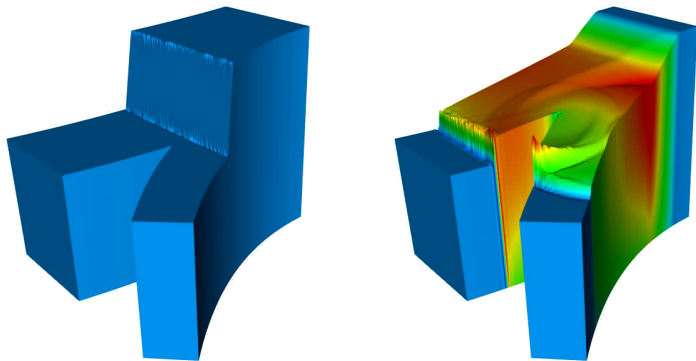


Figure: (Left) 3D representation of initial conditions and (Right) solution to a latter time

Introduction

Design and Implementation of DUNE PrismGrid

Numerical Results and Applications

Conclusion

Conclusion

- ▶ Meta grids increase the number of grids available in DUNE
- ▶ PrismGrid: meta grid with prismatic elements and additional functionality (*iterators, host grid acces*)
- ▶ Importance of generic reference elements for meta grids

Outlook

- ▶ Parallelization
- ▶ Adaptivity
- ▶ Performance
- ▶ Documentation
- ▶ ...

Thank you for your attention!

Conclusion

- ▶ Meta grids increase the number of grids available in DUNE
- ▶ PrismGrid: meta grid with prismatic elements and additional functionality (*iterators, host grid acces*)
- ▶ Importance of generic reference elements for meta grids

Outlook

- ▶ Parallelization
- ▶ Adaptivity
- ▶ Performance
- ▶ Documentation
- ▶ ...

Thank you for your attention!

Conclusion

- ▶ Meta grids increase the number of grids available in DUNE
- ▶ PrismGrid: meta grid with prismatic elements and additional functionality (*iterators, host grid acces*)
- ▶ Importance of generic reference elements for meta grids

Outlook

- ▶ Parallelization
- ▶ Adaptivity
- ▶ Performance
- ▶ Documentation
- ▶ ...

Thank you for your attention!